Mathematical Tools for Neural and Cognitive Science

Fall semester, 2017

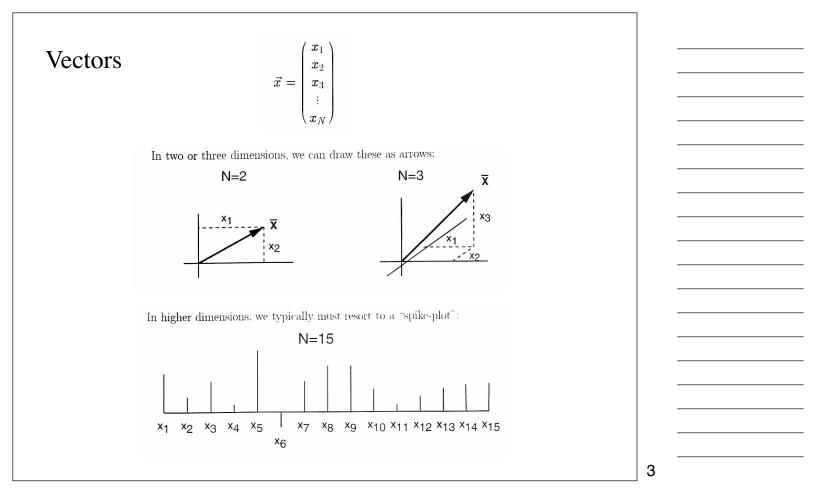
Section 1: Linear Algebra

Linear Algebra

"Linear algebra has become as basic and as applicable as calculus, and fortunately it is easier"

- Gilbert Strang, Linear Algebra and its Applications

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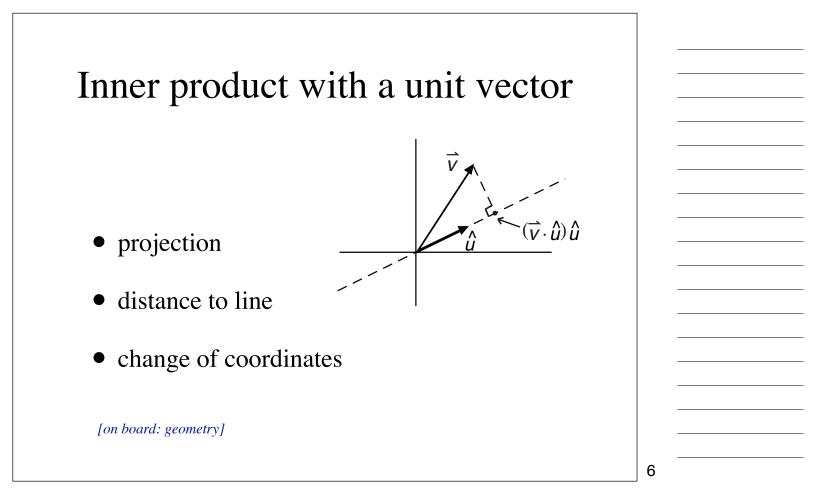
Vector operations

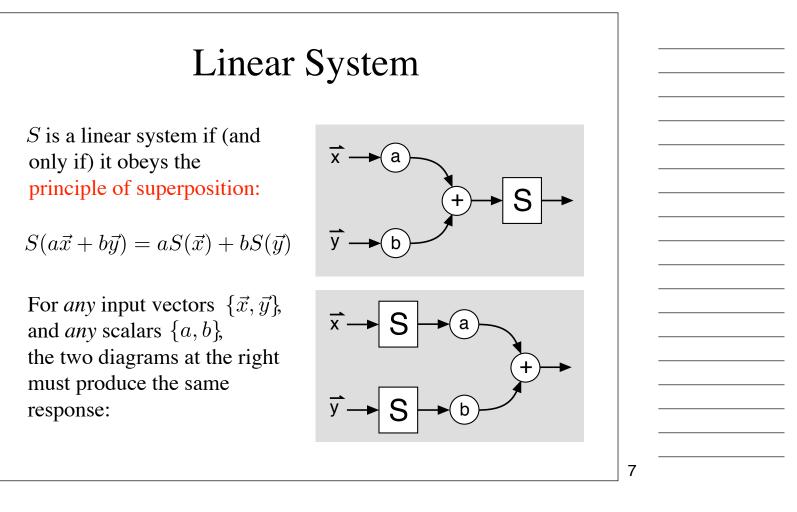
- scalar multiplication
- addition, vector spaces
- length, unit vectors
- inner product (a.k.a. "dot" product)
 - properties: commutative, distributive
 - geometry: cosines, orthogonality test

[on board: geometry]

Weeten and a weetager" "windowed averager" "gaussian averager" "local differencer" "component selector"

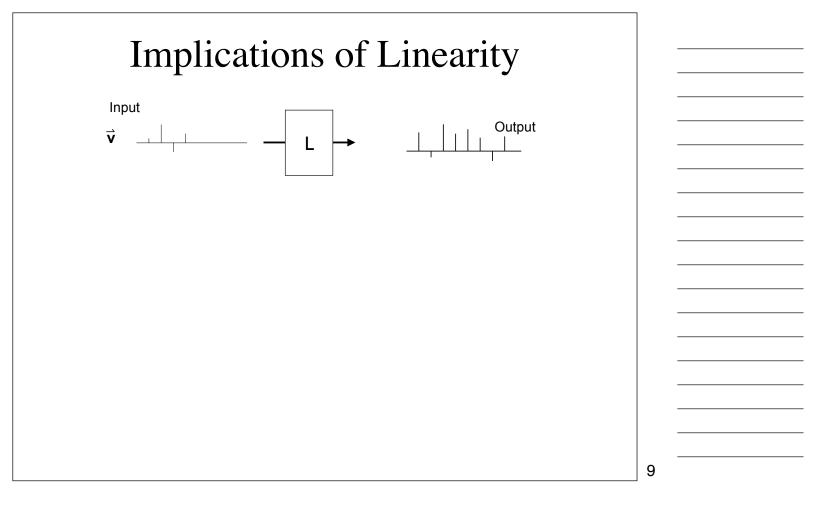


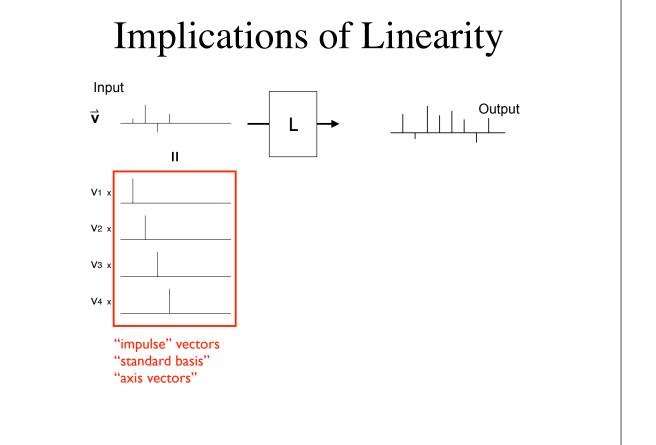


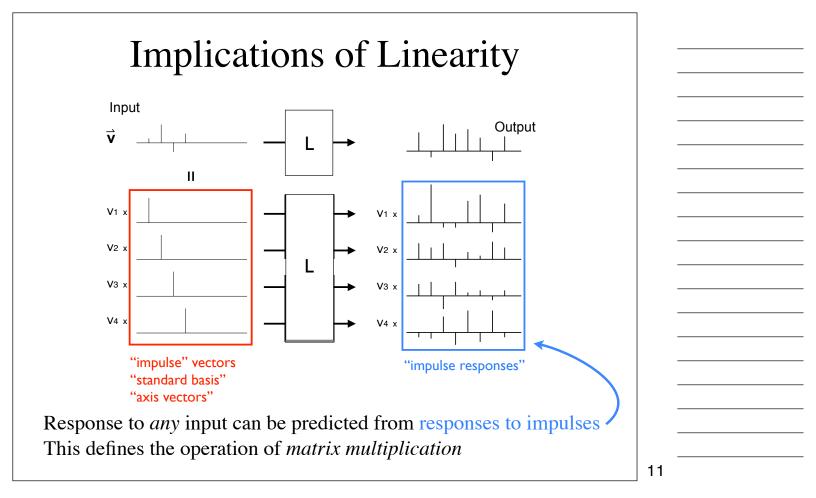


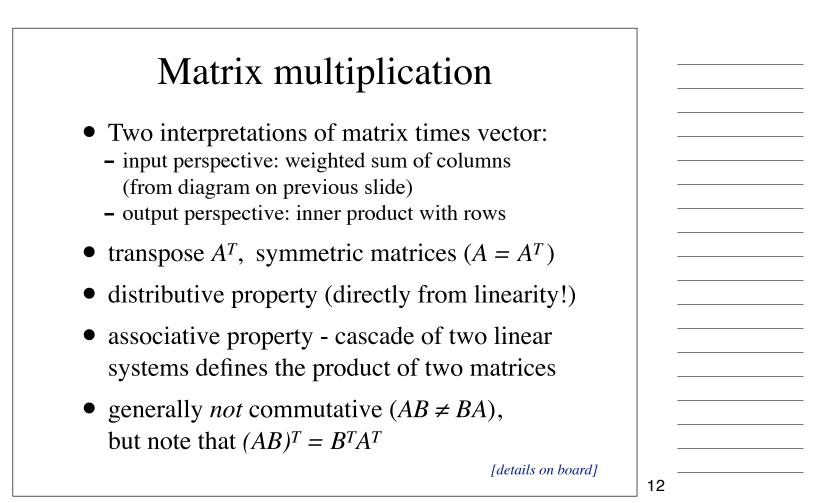
Linear Systems

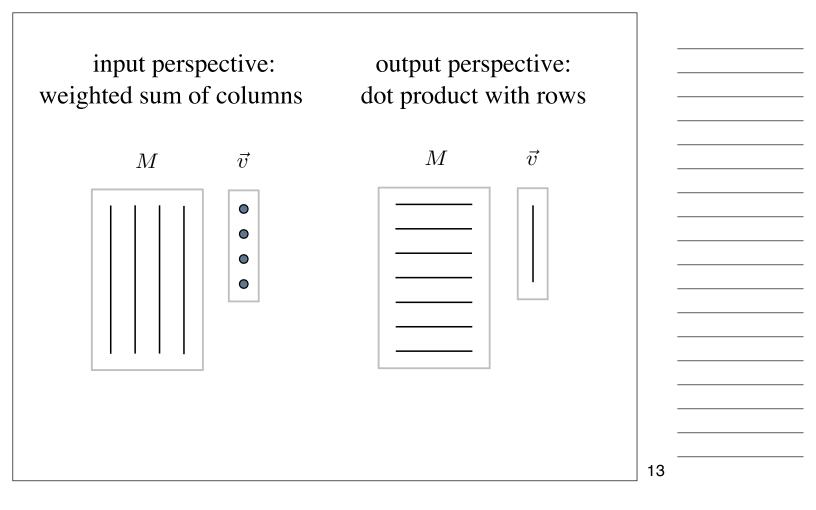
- Very well understood (150+ years of effort)
- Excellent design/characterization toolbox
- An idealization (they do not exist!)
- Useful nevertheless:
 - conceptualize fundamental issues
 - provide baseline performance
 - good starting point for more complex models

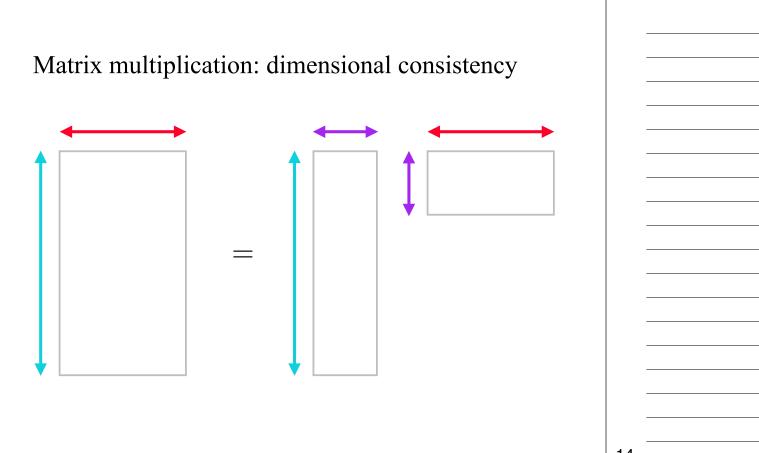


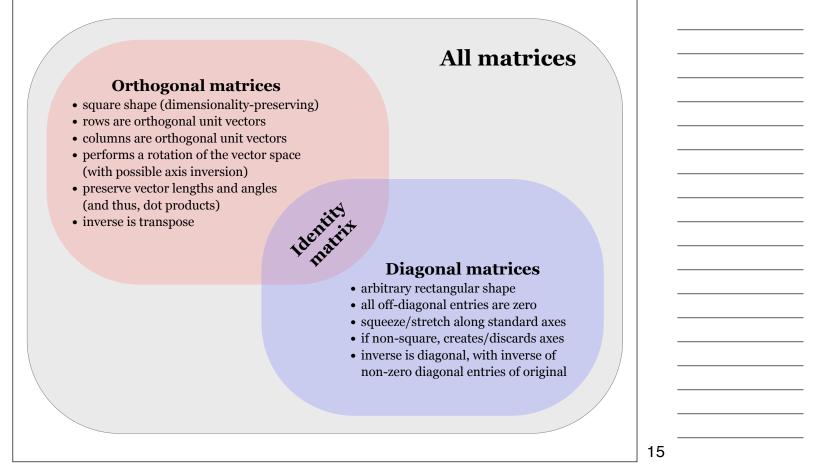












Singular Value Decomposition (SVD)

- M = U S V^T, "rotate, stretch, rotate"
 columns of V are basis for input coordinate system
 columns of U are basis for output coordinate system
 S rescales axes, and determines what gets through
 interpretation as sum of "outer products"
 non-uniqueness (permutations, sign flips)
- nullspace and rangespace
- inverse and pseudo-inverse

[details on board]

