Vision and the statistics of the visual environment
Eero P Simoncelli

It is widely believed that visual systems are optimized for the visual properties of the environment inhabited by the organism. A specific instance of this principle is known as the Efficient Coding Hypothesis, which holds that the purpose of early visual processing is to produce an efficient representation of the incoming visual signal. The theory provides a quantitative link between the statistical properties of the world and the structure of the visual system. As such, specific instances of this theory have been tested experimentally, and have been used to motivate and constrain models for early visual processing.

Addresses
4 Washington Place, Room 809, New York, NY 10003-6604, USA
e-mail: eero.simoncelli@nyu.edu

Abbreviations
V1 primary visual cortex

Introduction
One of the primary roles of theory in the sciences is to provide fundamental principles that explain why the natural world is constructed as it is. In biology, the main example of such a principle is the theory of evolution by natural selection. In the context of vision, this sort of philosophy was championed by Marr [1], who argued that it is essential to consider the visual system at an abstract computational level in order to understand its design.

Two specific instances of this philosophy provide a quantitative link between the statistical properties of the visual environment and the structure of biological visual systems: the so-called Efficient Coding Hypothesis, and the formulation of early vision problems in terms of Bayesian estimation or decision theory. Specific instances of both theories can be tested experimentally, and can be used to motivate and constrain models for vision. The Efficient Coding Hypothesis has been a central topic in a variety of recent workshops and meetings (see box 1), as well as of several review articles [2,3••] and a special journal issue [4]. Recent results related to this hypothesis are interesting although controversial. Owing to this flurry of recent interest, and because

Bayesian theories of vision have been reviewed in several other places (e.g. [5–10]), I focus almost entirely on efficient coding in this review, with the emphasis on studies published over the past two years.

Efficient coding
The theory of information plays a natural role in models of neural systems by providing abstract but unique quantitative definitions for information [11]. Barlow [12] recognized the importance of information theory in this context and hypothesized that the efficient coding of visual information could serve as a fundamental constraint on neural processing. This hypothesis holds that a group of neurons should encode information as compactly as possible, so as to utilize the available computing resources most effectively. Mathematically, this is expressed as a desire to maximize the information that neural responses provide about the visual environment.

The simplest form of this hypothesis (in particular, ignoring the noise in neural responses) decouples naturally into two separate statements: one regarding the statistics of individual neural responses and a second regarding the joint statistics of the responses of a population of neurons [2,13,14]. The responses of an individual neuron to the natural environment should fully utilize its output capacity, within the limits of any constraints on the response (e.g., maximum firing rate). In other words, each neuron should utilize its full output capacity in encoding information. The responses of different neurons to the natural environment should be statistically independent from each other. In other words, the information carried by each neuron should not be redundant with that carried by the others. This is also consistent with a notion that the visual system strives to decompose a scene into statistically independent constituents (e.g. individual objects). More detailed discussions of these ideas, as well as the role of noise, may be found in other articles [2,12,14–21].

Criticisms
A variety of criticisms have been voiced regarding the Efficient Coding Hypothesis. Several of these represent misconceptions about the theory, some are aimed at particular variants of the theory, some are about practical experimental issues, whereas others are more fundamental. Below is brief discussion of some of these criticisms (see the recent review article by Barlow [3••] for additional discussion).

The purpose of vision
It has often been argued that efficient coding of visual information is irrelevant because the purpose of vision is

not to encode or reconstruct the visual world. There is some truth to this criticism, in that the hypothesis does not take into account how the information that has been extracted is to be used. This may be viewed as either an advantage (because one does not need to assume any specific visual task or goal, and does not even need to specify what is being represented) or a limitation (because tasks and goals are clearly relevant for visual processing). More complete theories, such as that given by Bayesian estimation and decision, can take into account both the statistical structure of the environment and the visual task or goal.

Relevance of information theory
A second criticism of the Efficient Coding Hypothesis is that 'information theory is irrelevant because the brain is not concerned with bits'. Bits are simply a standard choice of unit for information, but the abstract definition of information is well motivated, unique, and most certainly relevant to the brain.

Experimentally observed dependency
One criticism of the Efficient Coding Hypothesis is that 'some experimental data from multi-neuron recordings show correlation, synchronization, or other forms of statistical dependency between neurons'. Most of these data came from experiments that did not use naturalistic stimuli, however, and thus dependencies in the neural responses are not directly relevant to the hypothesis. In addition, recent studies suggest that responses to natural stimuli in the primary visual cortex (V1) are relatively independent [22,23•,24•]. Even if one were to observe dependencies in neural responses under natural stimulus conditions, the hypothesis states only that the system strives for independence; the constraints of neural processing may prevent this being achieved. Taking this into account, a more realistic expectation might be that successive stages of processing (e.g. steps along an ascending sensory pathway) should reduce statistical dependence [25••].

Over-representation in cortex
A further criticism of the Efficient Coding Hypothesis is based on a comparison of the number of retinal ganglion cells to the number of neurons in the primary visual cortex. Critics argue that 'the number of neurons devoted to processing sensory information seems to expand as one goes deeper into the system, suggesting that the brain increases redundancy'. This argument usually assumes, however, that the coding capacity of all neurons (and in particular those in retina and cortex) is the same. The distribution of information amongst more neurons does not necessitate more redundancy if the form of neural coding employed by those neurons differs. For example (as Barlow points out [3••]), cortical neurons tend to have lower firing rates than retinal neurons, and may well use a different form of code. In addition, cortical neurons have more complex temporal dynamic properties (e.g. adaptation) that may serve to encode information over longer timescales. Although the redundancy of retinal and V1 neurons has not been experimentally compared, a related comparison in the auditory system was able to demonstrate a reduction of redundancy [25••].

Experimental impracticality
Estimation of information-theoretic quantities requires enormous amounts of data, and is thus impractical for experimental verification. This is a significant problem for the Efficient Coding Hypothesis, especially as commonly used estimators of information are known to be heavily biased. Nevertheless, cases of successful experimental measurement give reason for optimism on this point (see below).

Definition of input and output
The Efficient Coding Hypothesis crucially depends on the probability distribution of natural images and the definition of the neural response, both of which are unconstrained. Thus, the theory is not as assumption free as one is led to believe. In my opinion, this is the most fundamental problem with the hypothesis. Typically, the input distribution is not defined explicitly, but is assumed to be well represented by a collection of calibrated 'naturalistic' images. When applying the hypothesis, one must specify which neurons are meant to satisfy the hypothesis (e.g., neurons within a particular cell class, or within a specific visual area, or across multiple visual areas), and how their responses are to be measured (e.g. mean firing rates versus individual spike times). Again, examples of successful experimental measurement give us reason for optimism.

Importance of noise
The final criticism of the Efficient Coding Hypothesis discussed here is that 'commonly used versions of the theory that ignore noise and other physical constraints are too simplistic'. This is a valid argument, but in many cases may not constitute a fatal flaw. Even simplistic forms of the theory seem to make interesting predictions, and many authors have developed more sophisticated versions that include physical constraints such as noise (see below).

Testing the hypothesis

Although the Efficient Coding Hypothesis is roughly fifty years old, it has only recently been explored quantitatively. This recent progress is due to three fundamental improvements in the field. First, we have a much better understanding of early sensory processing. Second, mathematical and engineering tools have been developed for the description and manipulation of more complex statistical models. And third, advances in computing and imaging technologies allow us to gather and manipulate vast quantities of image data, both for use as experimental stimuli and for statistical modeling purposes.

There are two basic methodologies for testing and refining the Efficient Coding Hypothesis. The direct approach is to examine the statistical properties of neural responses under natural stimulation conditions (e.g. [20,22,26–28]). An alternative approach is to use the statistical properties of natural images to constrain or derive a model for early sensory processing (e.g. [18,29–37]). Below, I review some recent examples of each of these methods.

Experimental tests

In recent years, there have been several interesting experimental studies that take the direct approach and examine neural responses to naturalistic images or image sequences (see [38••] for a review). Researchers have measured efficiency in a variety of different ways, and although the results of some studies seem to confirm the hypothesis of efficient coding, others seem inconsistent with it. On the whole, however, recent results have helped to advance our understanding of the issues under investigation.

For example, Baddeley et al. [28] had shown that firing-rate distributions of cat visual area V1 neurons and monkey inferotemporal (IT) neurons were exponential under naturalistic conditions, which implies optimal information transmission for a fixed average rate of firing. A subsequent study of monkey IT neurons found that only a minority were well described by an exponential firing distribution [39]. De Polavieja [40] later argued that this discrepancy was due to the fact that the exponential solution is correct only for the noise-free case, and showed that by taking noise into consideration, one could account for the observed results.

Similarly, previous results from Meister et al. [41] suggested that retinal ganglion cells exhibit strong firing correlations, and that these patterns could provide useful information (although these experiments did not directly address efficient coding as they were not based on natural image stimuli). A recent article by Nirenberg et al. [23•] argues that retinal ganglion cells act as independent encoders, on the basis of multi-cell recordings with natural stimuli and a novel (but controversial) choice of

redundancy measure. Reich et al. [42•] found that responses of V1 neurons are nearly independent under non-natural (approximately white noise) stimulation. This seems inconsistent with the Efficient Coding Hypothesis, as one typically expects efficiency to degrade for non-natural stimuli (e.g. [20]). Wiener et al. find that the information encoded by the spike counts of V1 neurons over moderate length intervals is nearly the same for various artificial stimuli as it is for naturalistic stimuli [43]. Vinje and Gallant [24•] recently reported that the presence of natural stimuli in the non-classical receptive field increases several measures of informational efficiency. Finally, it is worth mentioning an interesting article by Chechik et al. [25••], even though the study concerns the auditory system. Their work provides one of the first direct tests of the reduction of redundancy as one ascends a sensory pathway.

Several studies suggest that the visual system exhibits improved performance under naturalistic input conditions. For example, Lewen et al. [44] demonstrated that the H1 neuron in the blowfly responds over a substantially broader range of velocities for outdoor scenes than for indoor scenes. Kern et al. [45] show that blowfly neurons can encode turning directions independently of environmental texture and spatial structure, but only when the environment is 'natural'. Although the connection has not been fully established, the Efficient Coding Hypothesis suggests that optimal characterization of a neural system might be best performed using naturalistic stimuli. Experiments to demonstrate this have been performed (e.g. [46]), and recently developed analysis techniques may provide the necessary tools for characterization [47,48].

Optimal models

As mentioned above, the second method of testing the Efficient Coding Hypothesis is to derive a model for the efficient coding of the environment and then compare it with physiological data. Many of the original attempts to use this method were constrained to linear filtering and second-order statistical modeling (e.g. [18,29–33]). Recently, several authors have established relationships between higher-order statistical properties and linear filtering (e.g. [34,35]). Others have also used various forms of non-linear processing, such as divisive gain control [37,49•–51•]. In addition, some authors are beginning to explore the cascades of redundancy-reduction stages. For example, Hoyer and Hyvarinen [52•] have developed a model that forms contour-like receptive fields on the basis of the statistical properties of model V1 complex cell responses under natural stimulus conditions.

Extensions

Researchers have recently used a variety of auxiliary constraints or extensions to augment the efficiency hypothesis. Several authors have tried to incorporate

the metabolic costs of neural activity as a constraint [53,54]. Recently, Balasubramanian and Berry [55] demonstrated that retinal ganglion cells in the tiger salamander are optimized to transmit visual information at a minimal metabolic cost, assuming that the symbols of the neural code are represented by spike bursts of a given length. Although this result is interesting, the data were recorded under artificial visual stimulation conditions, and thus do not bear directly on the issue of environmental statistics. Similarly, Gottschalk [56] shows that a hyperbolic ratio provides an optimal neural response to non-linearity, in that it maximizes information transmission subject to a simple model of neural costs that includes both synaptic strength and spike rate. Again, the result is implicitly based on white noise input stimuli, and thus does not bear directly on the Efficient Coding Hypothesis.

It has been proposed that efficient coding might also apply to adaptive processes [57–59]. Brenner *et al.* and Fairhall and co-workers [60,61•] have demonstrated that adaptation of the fly's H1 neuron to the variance of a white-noise stimulus appears to optimize information transmission.

Several other authors have also augmented efficient coding with other constraints or principles. Several authors have derived models for V1 complex cells by maximizing the independence or temporal coherence of cells constructed using non-linear combinations of linear subunits (e.g., sums of squared linear filter responses) [62–64]. Balboa and Grzywacz [65] argue that lateral inhibition in the retina is inconsistent with pure information maximization, and provide an alternative hypothesis suggesting that the system is designed to detect and represent image features in the presence of photon-absorption noise. Additionally, Von-de-Twer and Mcleod [66] showed that color representation in monkey ganglion cells is best understood in the context of optimizing the average ability to discriminate color signals in the natural environment.

Conclusions
The recent resurgence of interest in efficient coding has produced several interesting experimental and theoretical results. Rather than merely solidifying or disproving the basic hypothesis, however, this body of work demonstrates the complexity and subtlety of establishing a firm quantitative connection between the properties of natural stimuli and a neural response. Most of the difficulty lies in the definition of the input (what is a 'natural' image?) and the output (which neurons should be considered, and how does one define 'neural response'?), as well as in the complexities of incorporating realistic constraints (e.g. noise and metabolic costs) and computational goals. As we wrestle with these issues, it becomes clear that the value of efficient coding has already far exceeded its role

as a hypothesis to be evaluated. Effort directed at studying this hypothesis has significantly advanced the field by increasing the general level of quantitative investigation, by leading us to carefully study and model the visual environment from a statistical standpoint, by forcing us to consider the influence of environmental statistics on neural response, and by encouraging us to examine neural response to natural stimuli. Although it seems improbable that Efficient Coding will suffice as the sole principle for understanding sensory system design, it is clear that it will continue to play an important role.

Acknowledgements

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